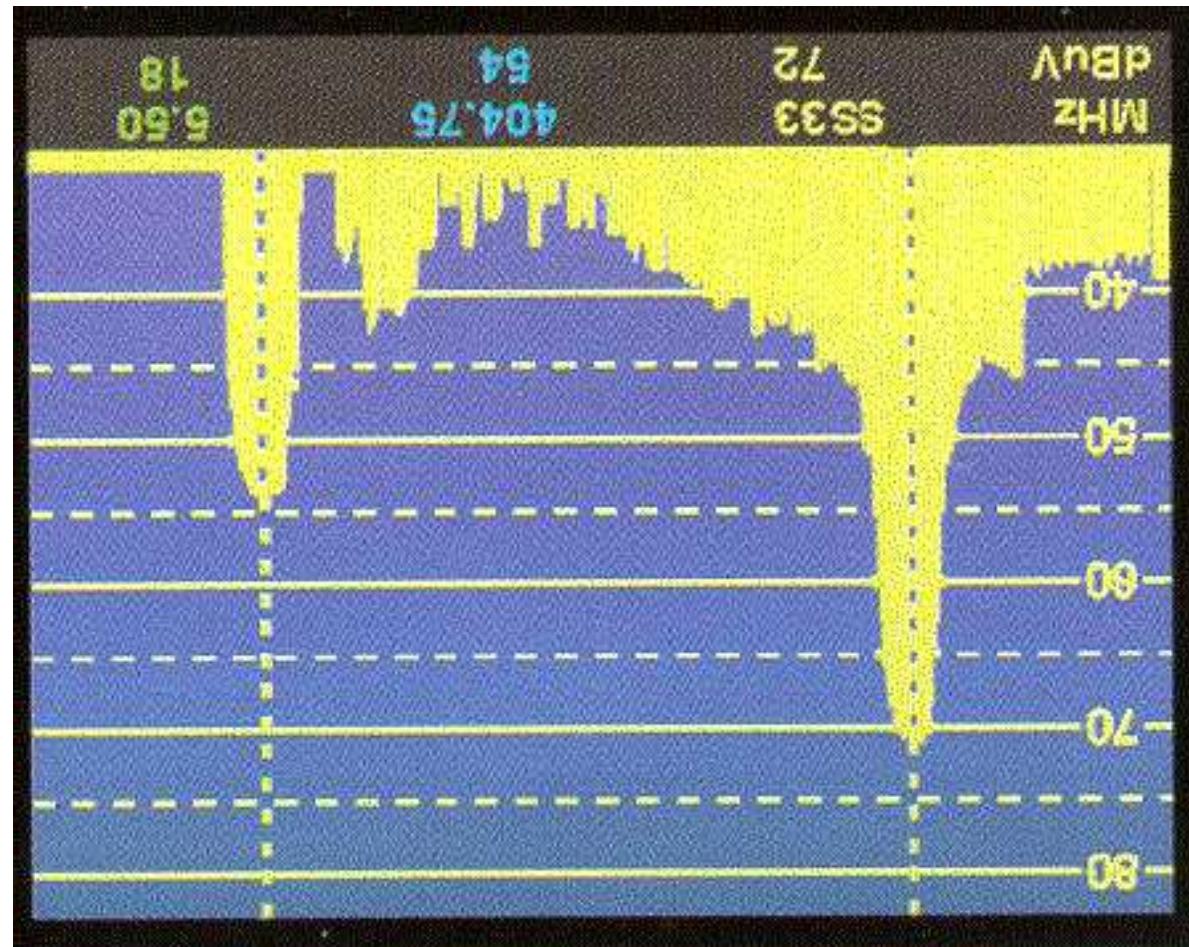


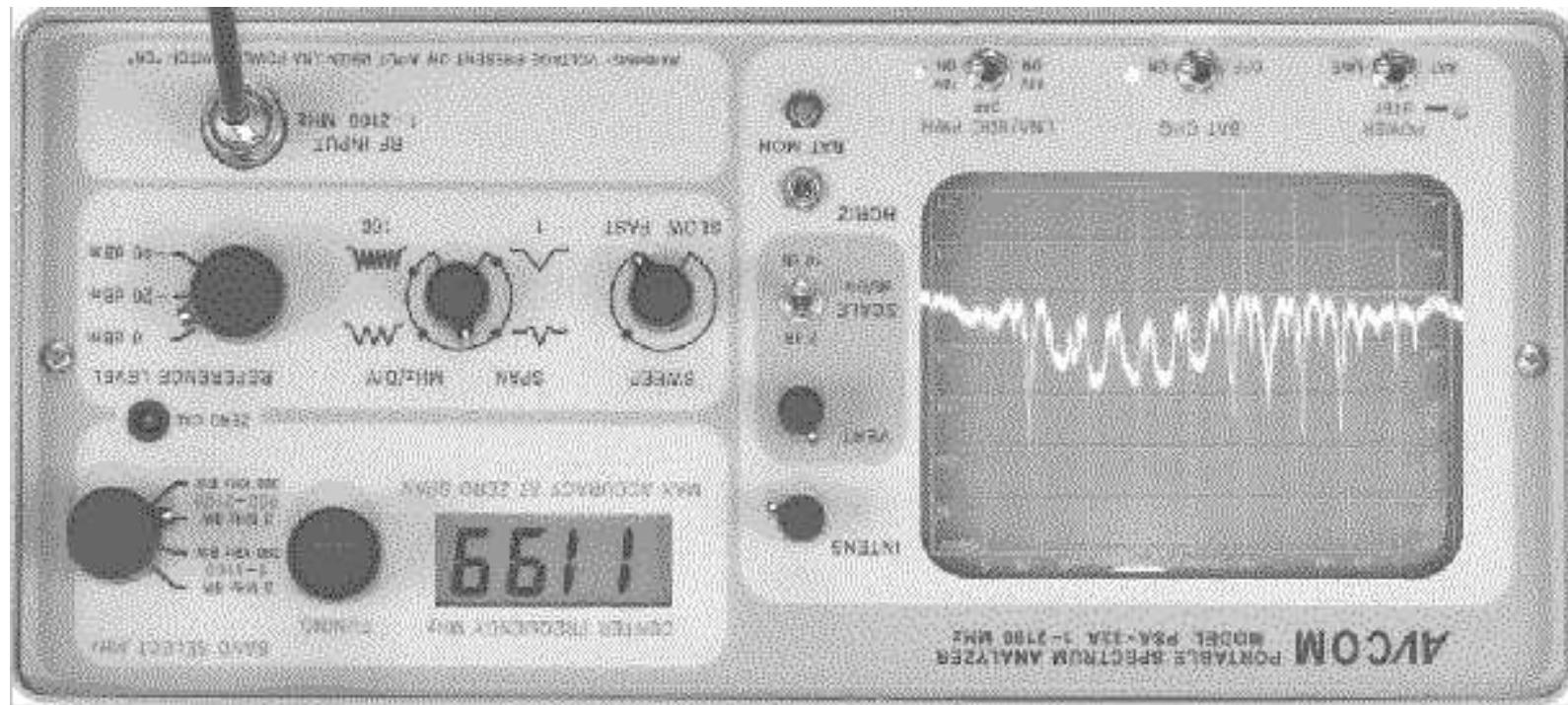
# Bandwidth Estimation Metrics and Terminology

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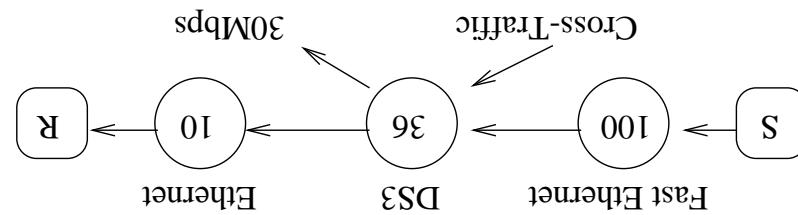


Bandwidth (Hz) versus Bandwidth (bps)

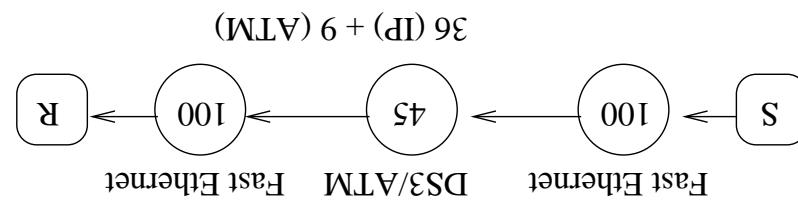


Bandwidth estimation in the physical layer

- Bulk-Transfer Capacity (BTC)

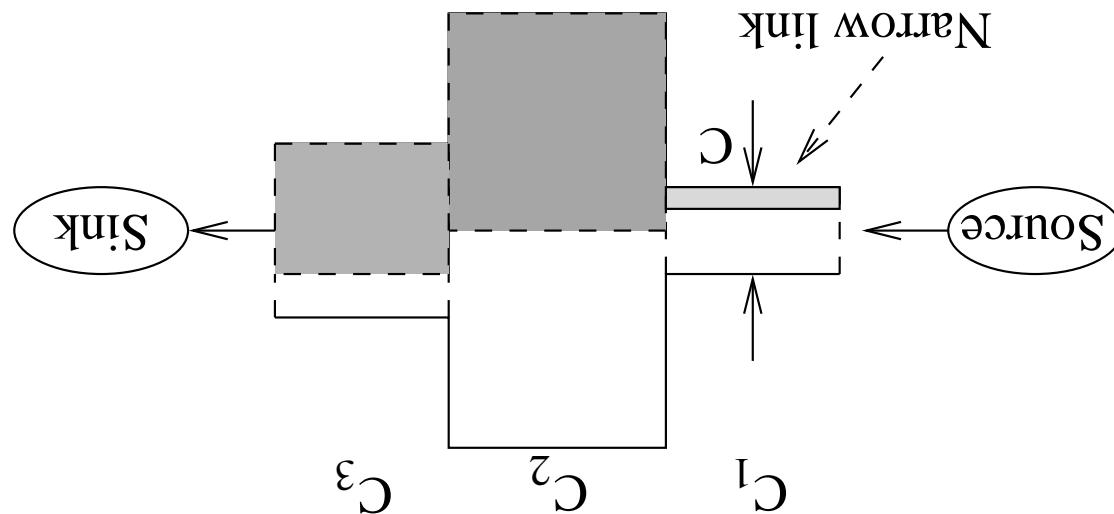


- Available bandwidth



- Capacity

Major bandwidth metrics



- Path capacity is limited by *narrow link*:

$$C = \min_{i=0 \dots H} \{C_i\} = C_n$$

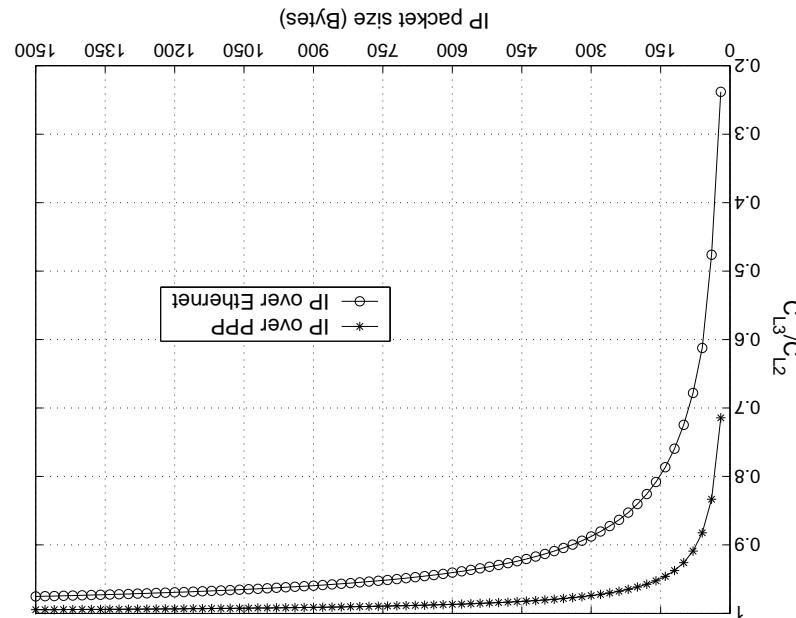
- Path capacity:

typically constant at layer-2, related to transmission clock

- Link capacity:  $C_i$  for link  $i$  (bps)

## Definition of capacity

- Beware of: traffic shapers, wireless links, time-varying capacity

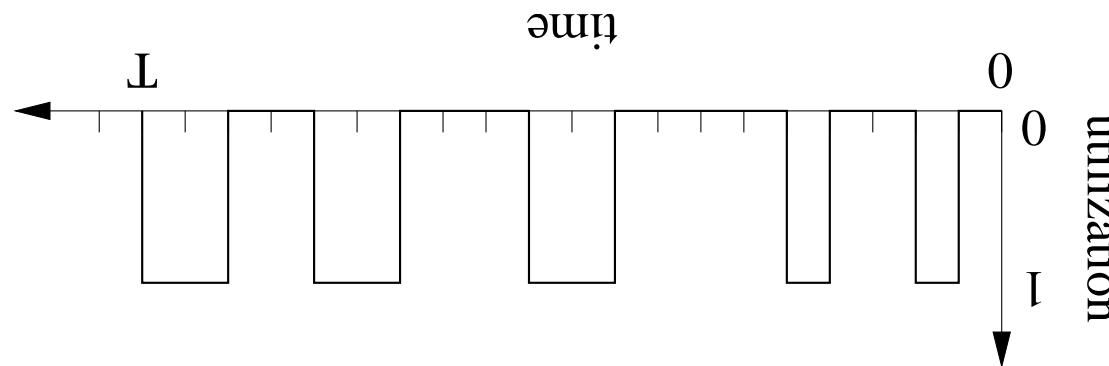


$$C_{L3} = \frac{L_{L3}}{\Delta L_3} = C_{L2} \frac{1 + \frac{H_{L2}}{L_{L3}}}{1}$$

- Capacity  $C_{L3}$  at IP-layer as function of  $C_{L2}$  at layer-2:

Capacity at IP-layer

- Note: variance of random process  $\underline{u}_T$  decreases with  $T$

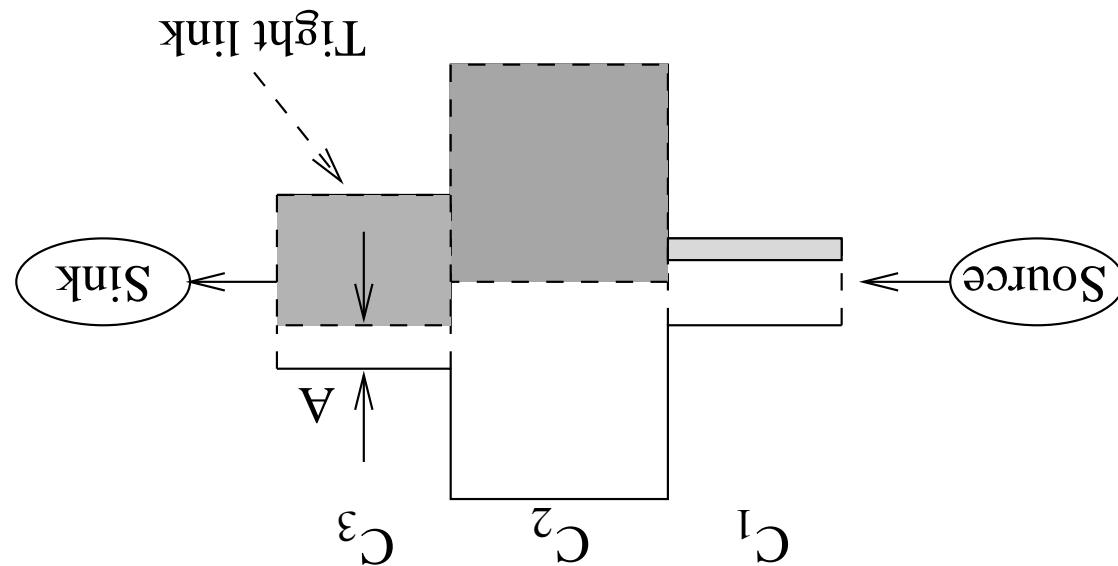


$$xp(x)u(t-\tau) = \frac{1}{T} \int_t^{t-T}$$

- Average utilization  $\underline{u}_T(t)$  in timescale  $T$ :
- Instantaneous link utilization  $u(x) \in \{0, 1\}$

Definition of average link utilization

- Available bandwidth is limited by *tight link*



$$\text{End-to-end avail-bw: } A_{\tau} = \min_{i=0 \dots H} A^{i,\tau} = \min_i C^i (1 - u^{i,\tau})$$

- Avail-bw of link  $i$ :  $A^{i,\tau} = C^i (1 - u^{i,\tau})$

- $u^{i,\tau}$ : Average utilization of link  $i$  in time interval of length  $\tau$  ( $0 \leq u^{i,\tau} \leq 1$ )

## Definition of available bandwidth

- Bulk-Transfer Capacity (BTC): long-term average TCP throughput
- Congestion-limited transfer, i.e., sufficiently large receiver window
- BTC depends on:
  - Exact TCP implementation at sender & receiver
  - Available bandwidth
  - Link buffer sizes
  - Cross traffic responsiveness (elasticity)

## Bulk-Transfer Capacity definition

lossrate may be increased due to new TCP connection

- Note: such models cannot be used to predict BTC, because RTT and

$$\text{Throughput} = \frac{\text{RTT} \times \text{lossrate}}{\text{CMISS}}$$

- Simplest model:

- BTC can be derived mathematically

## BULK-Transfer Capacity estimation