

# The Subspace Method for Diagnosing Network-Wide Traffic Anomalies

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# What's happening in my network?

- Is my customer being attacked? probed? infected?
- Is there a sudden traffic shift?
- An external route change?
- A routing loop?
- An equipment outage?

Automated methods for reliably and generally answering such questions are lacking

# A General Framework

- We can treat all such problems as special cases of the general question:

Is my network experiencing **unusual** conditions?

- Then, adopt the following framework:
  - **Detection**  
Is there an unusual event?
  - **Identification**  
Which of the possible explanations fits best?
  - **Quantification**  
How serious is the problem?

# Statistical Approach

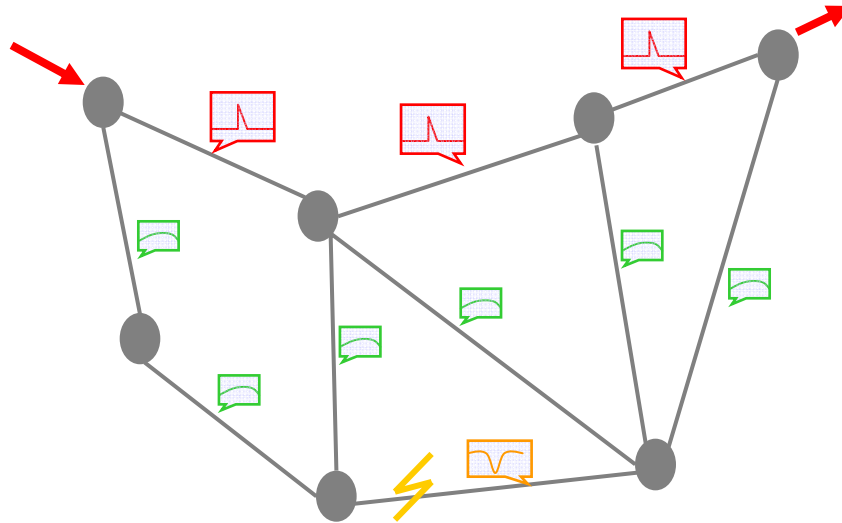
The advantage of such a framework is that it lends itself to a statistical approach:

- **Detection:** Outlier detection
- **Identification:** Hypothesis testing
- **Quantification:** Estimation



**Anomaly  
Diagnosis**

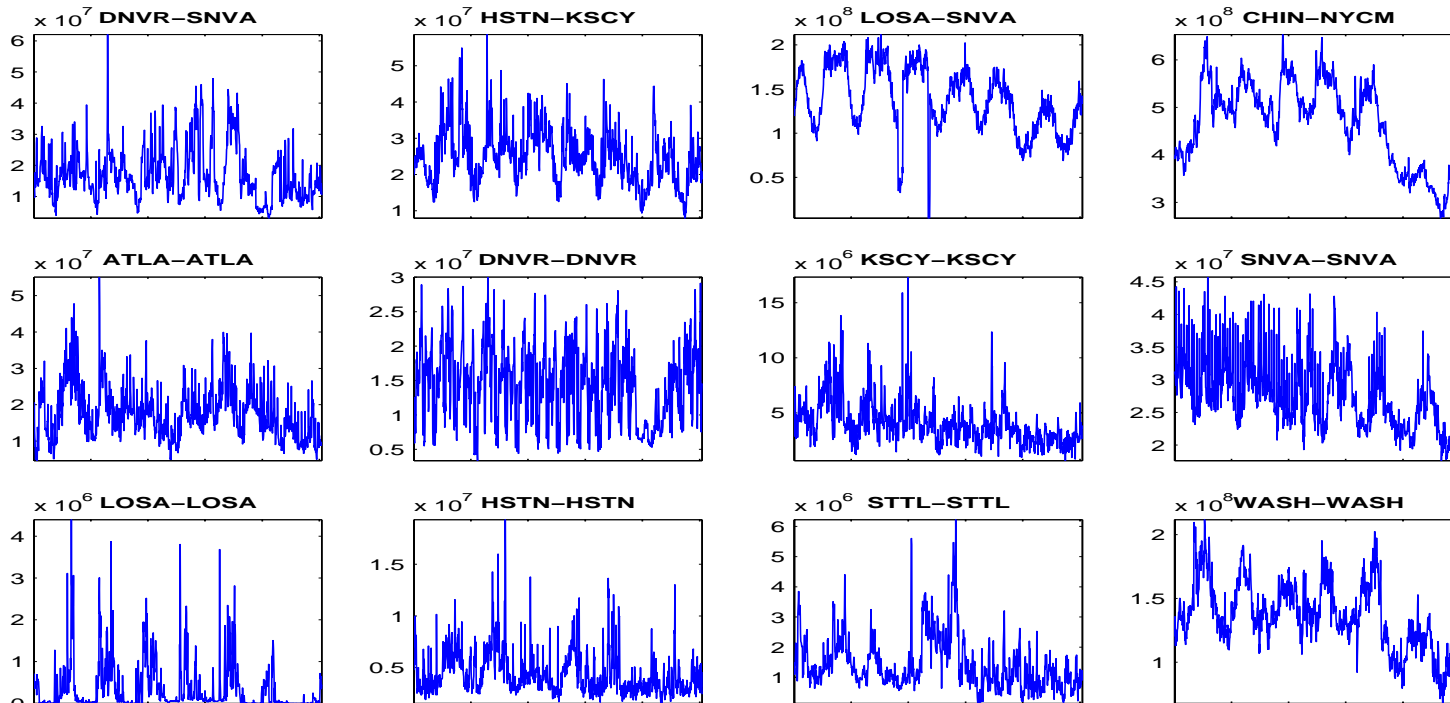
# A Need for Whole-Network Diagnosis



Our Thesis: Effective diagnosis of network anomalies requires a **whole-network** approach

For example, diagnosing traffic anomalies requires analyzing traffic from all links

# But, This Is Difficult!



How do we extract **meaning** from such a **high-dimensional** data in a systematic manner?

# Low Intrinsic Dimensionality of Link Traffic

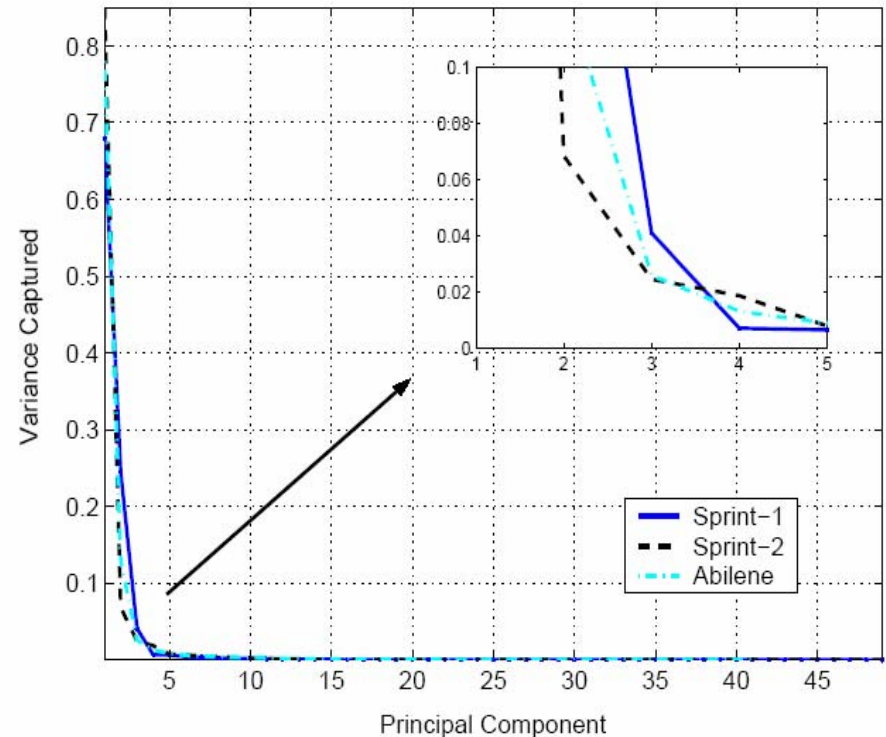
Studied via Principal Component Analysis

*Key result:*

Normal traffic is well approximated by a low dimensional space

*For example:*

Traffic on 40+ links is well approximated in space of only 4 dimensions



# Reasons for Low Dimensionality of Traffic

- Generally, traffic on different links is not independent
- Link traffic is the superposition of origin-destination flows (**OD flows**)
  - The same OD flow passes over multiple links, inducing correlation among links
  - All OD flows tend to vary according to common daily and weekly cycles, and so are themselves correlated

*[See SIGMETRICS 2004 paper]*



# The Subspace Method

- An approach to separate normal from anomalous traffic
- Define  $\mathcal{S}$  as the space spanned by the first  $k$  principal components
- Define  $\tilde{\mathcal{S}}$  as the space spanned by the remaining principal components
- Then, decompose traffic on all links by **projecting** onto  $\mathcal{S}$  and  $\tilde{\mathcal{S}}$  to obtain:

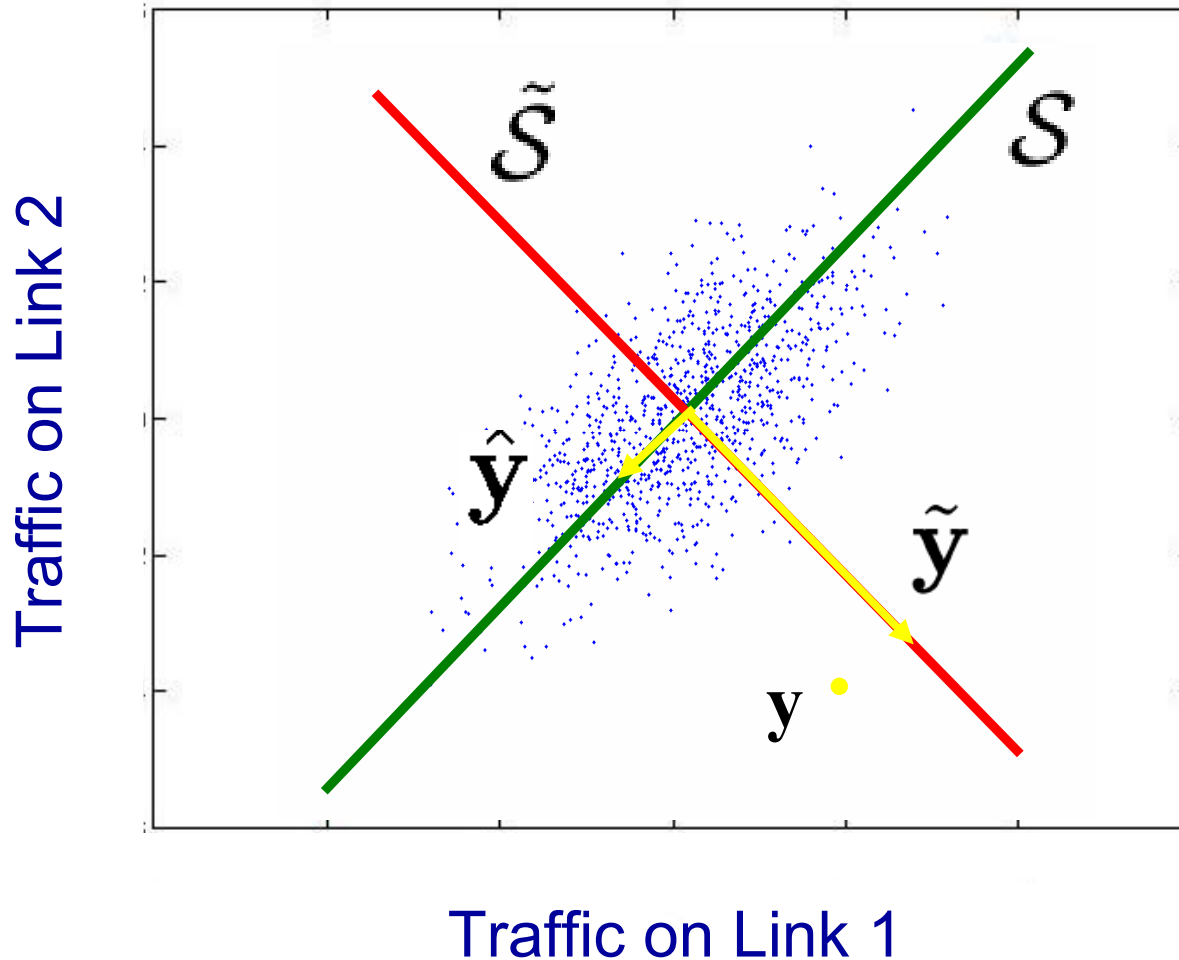
$$\mathbf{y} = \hat{\mathbf{y}} + \tilde{\mathbf{y}}$$

**Traffic vector of all links at a particular point in time** (blue text, blue arrow pointing to  $\mathbf{y}$ )

**Normal traffic vector** (green text, green arrow pointing to  $\hat{\mathbf{y}}$ )

**Residual traffic vector** (red text, red arrow pointing to  $\tilde{\mathbf{y}}$ )

# The Subspace Method, Geometrically



In general, anomalous traffic results in a large value of  $\tilde{y}$

$$\hat{y} = \mathbf{C}y$$

$$\tilde{y} = \tilde{\mathbf{C}}y$$

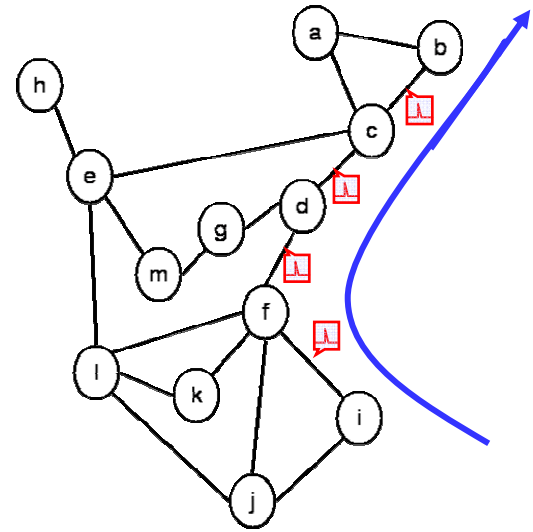
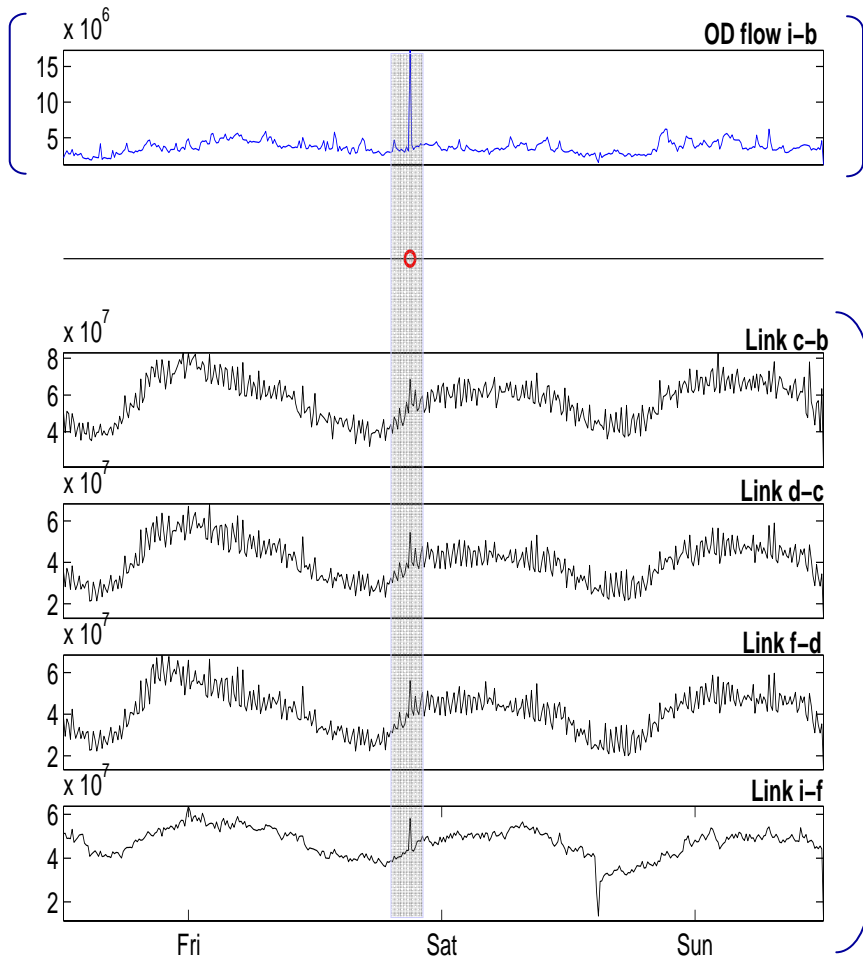
# Outline

- Subspace Method applied to Link Traffic
  - Problem: Volume Anomaly Diagnosis
  - Detection, Identification, Quantification
  - Validation
- Subspace Method applied to Flow Traffic
  - Problem: General Anomaly Detection
  - Sample Results
- Conclusions

# Diagnosing Volume Anomalies

- A ***volume anomaly*** is a sudden change in an OD flow's traffic (*i.e.*, point to point traffic)
- Problem Statement:  
Given link traffic measurements, diagnose the volume anomalies
- A first application of the subspace method

# An Illustration



Sprint-Europe Backbone Network

The *Diagnosis Problem* requires analyzing traffic on all links to:

- 1) **Detect** the time of the anomaly
- 2) **Identify** the source & destination
- 3) **Quantify** the size of the anomaly

# Subspace Method: Detection

- Error Bounds on Squared Prediction Error:

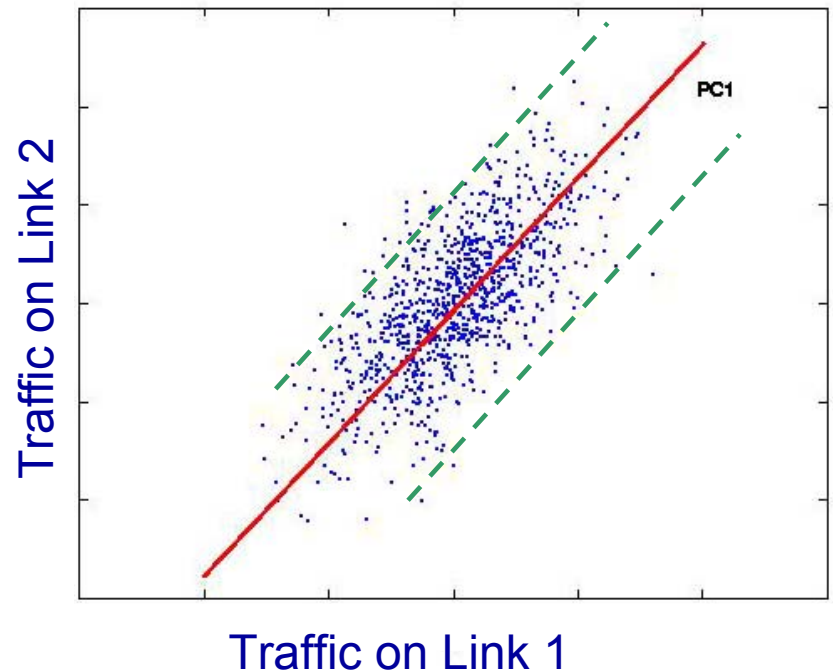
$$\text{SPE} \equiv \|\tilde{\mathbf{y}}\|^2 = \|\tilde{\mathbf{C}}\mathbf{y}\|^2$$

- Assuming multivariate Gaussian data, traffic is normal when,

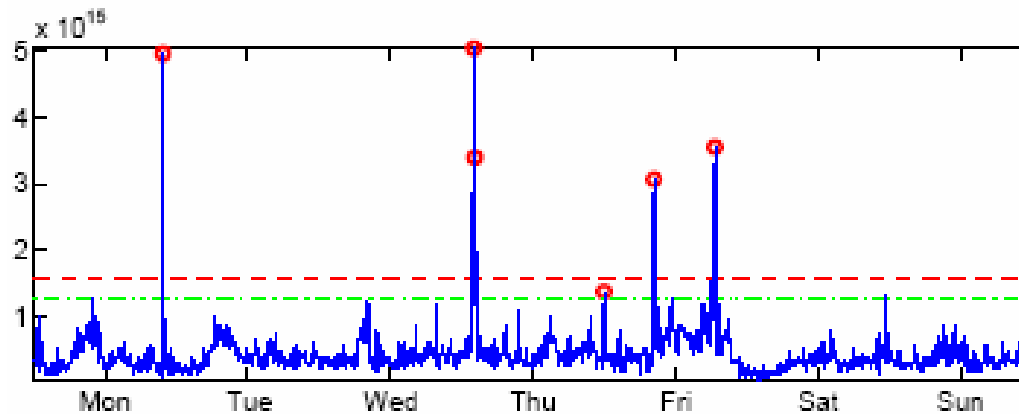
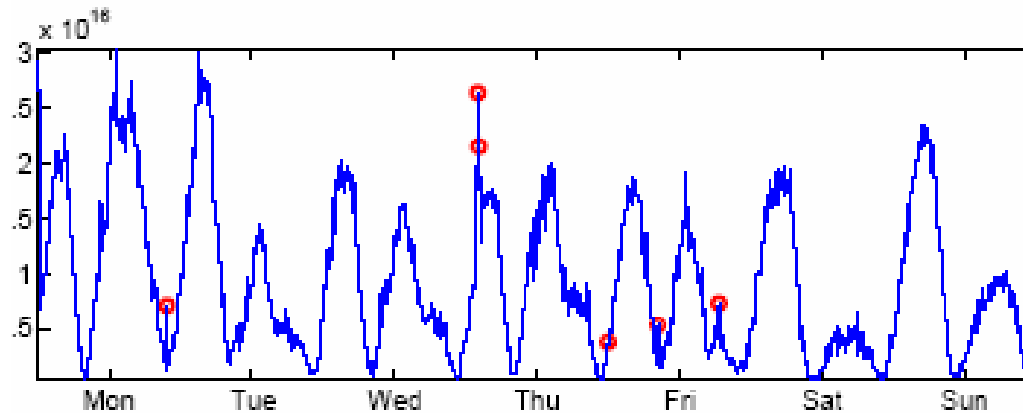
$$\text{SPE} \leq \delta_{\alpha}^2$$

Result due to

[Jackson and Mudholkar, 1979]



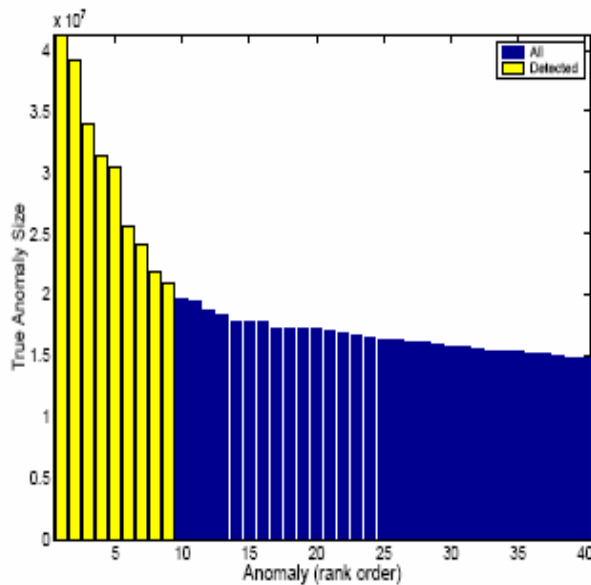
# SPE vs. All Traffic



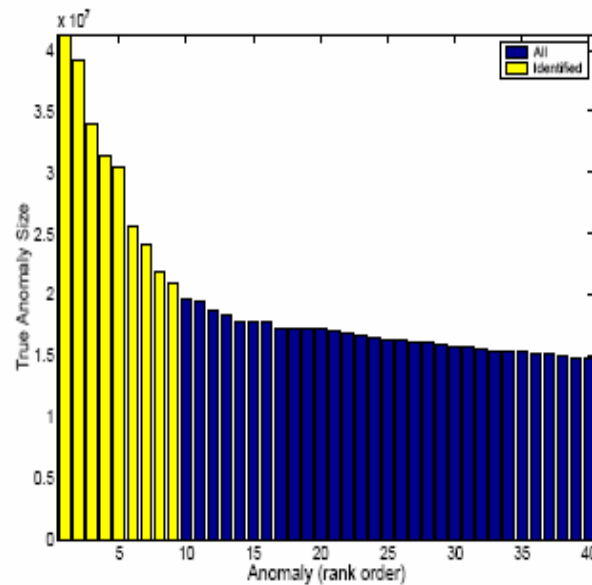
SPE ( $\|\tilde{\mathbf{y}}\|^2$ ) at anomaly time points clearly stand out

# Results on True Anomalies: Sprint-1

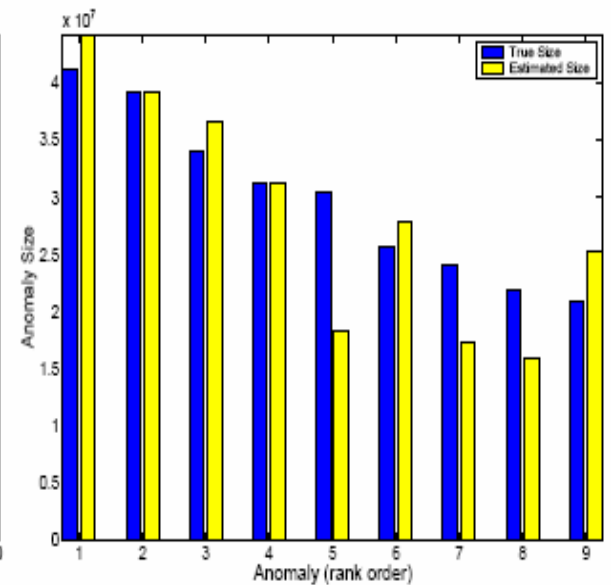
40 Largest deviations in OD flows via Fourier



Detection



Identification



Quantification

“Knee” in curve - natural cutoff for detection



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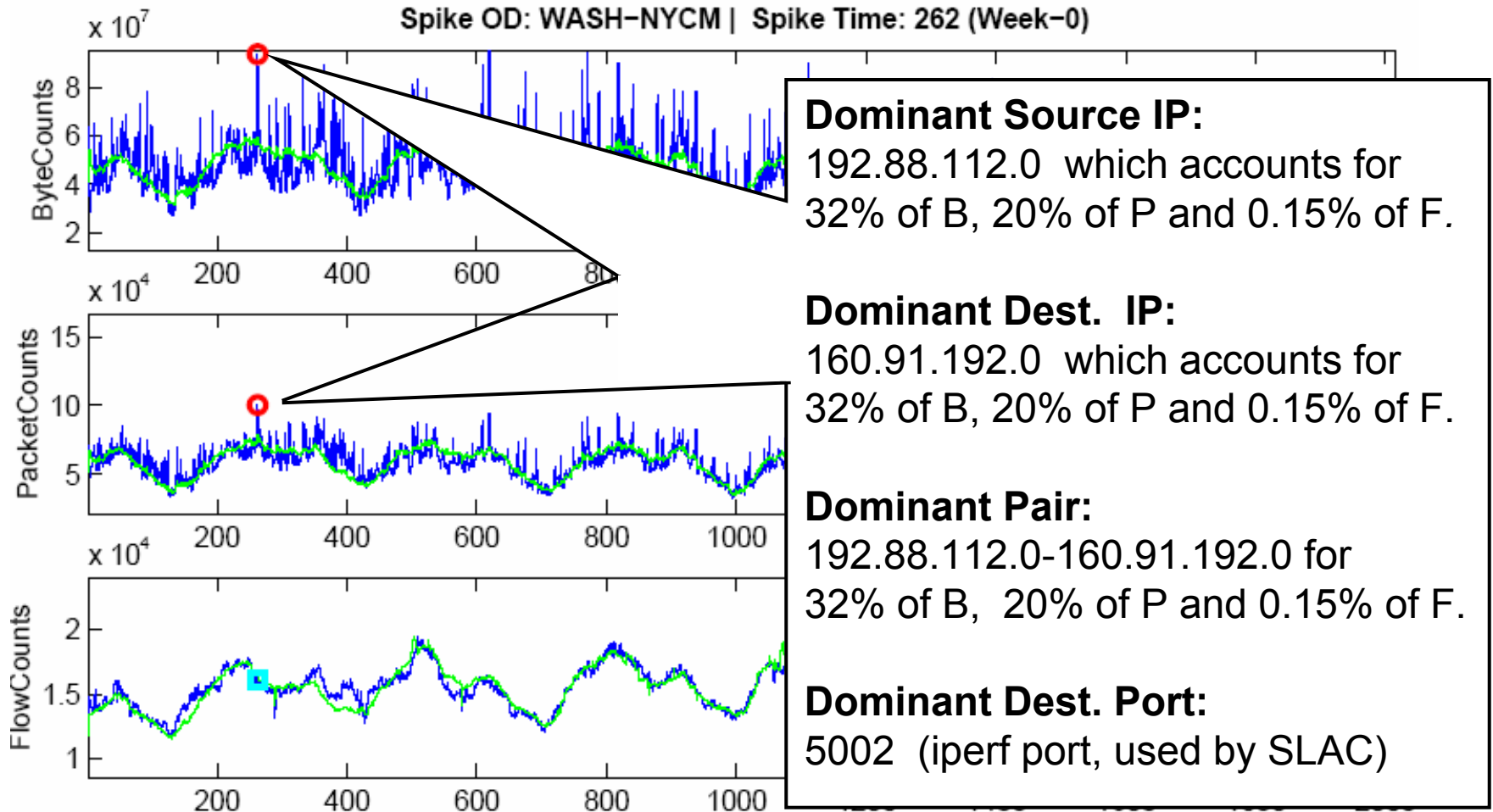
# Beyond Volume Anomalies

- Volume anomalies: important, but not the entire set of anomalies of interest to operators.
- Operators are also interested in:
  - DOS attacks, flash crowds, port scans, worm propagation, network equipment outages, changes in ingress/egress traffic patterns, ...
- Link data doesn't seem to hold enough information to accurately detect such a wide range of anomaly types.
- Therefore, we turn to **IP flow data**

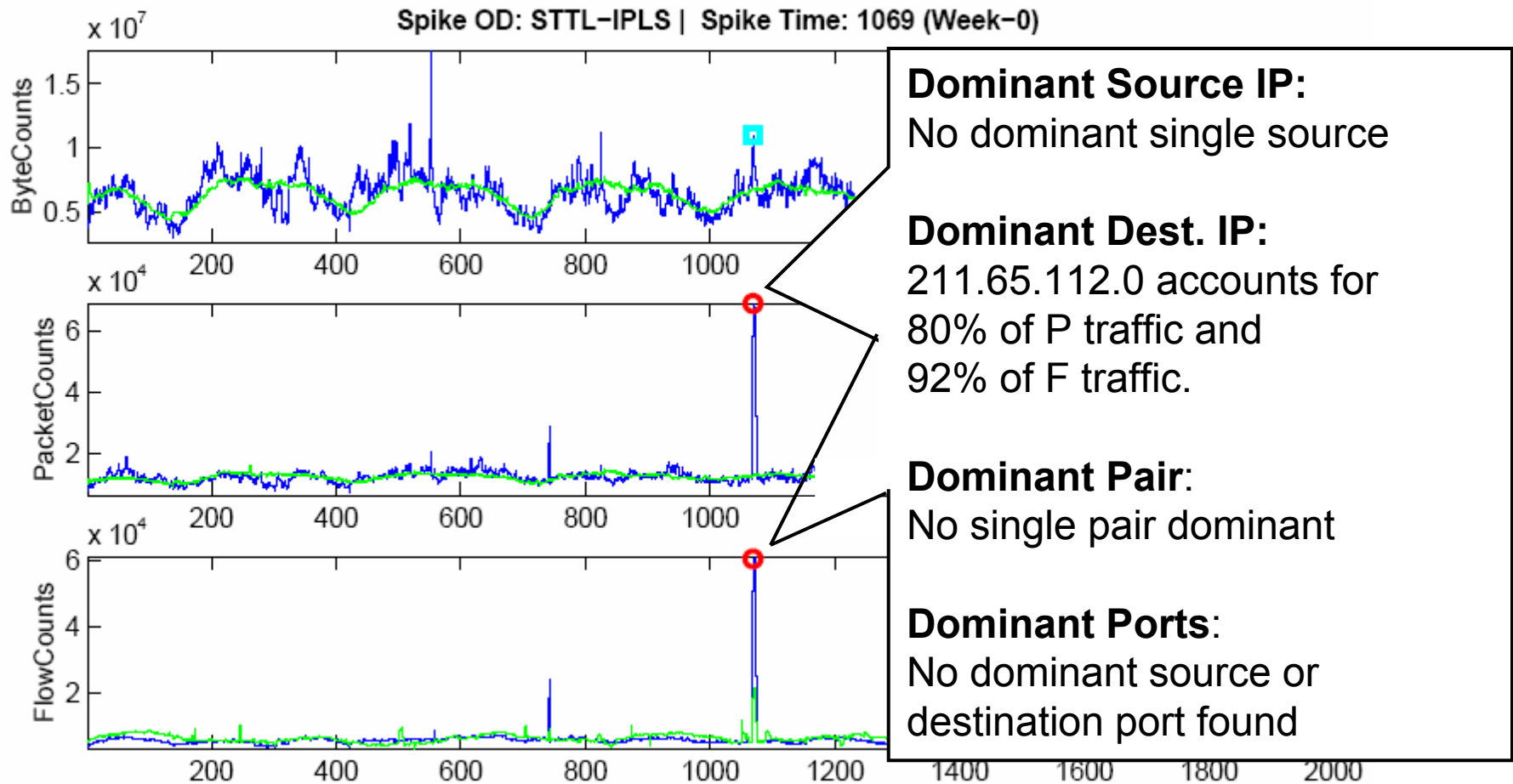
# Characterization Methodology

- Extend subspace method to diagnose anomalies directly in OD flow traffic timeseries
  - Detection in both  $\mathcal{S}$  and  $\tilde{\mathcal{S}}$  subspaces
- Examine OD flow traffic as three separate views: **# Bytes, # Packets, # IP-flows**
- Manually inspect each anomaly found over 4 week period in Abilene network
  - Using 5-tuple headers of sampled flow data

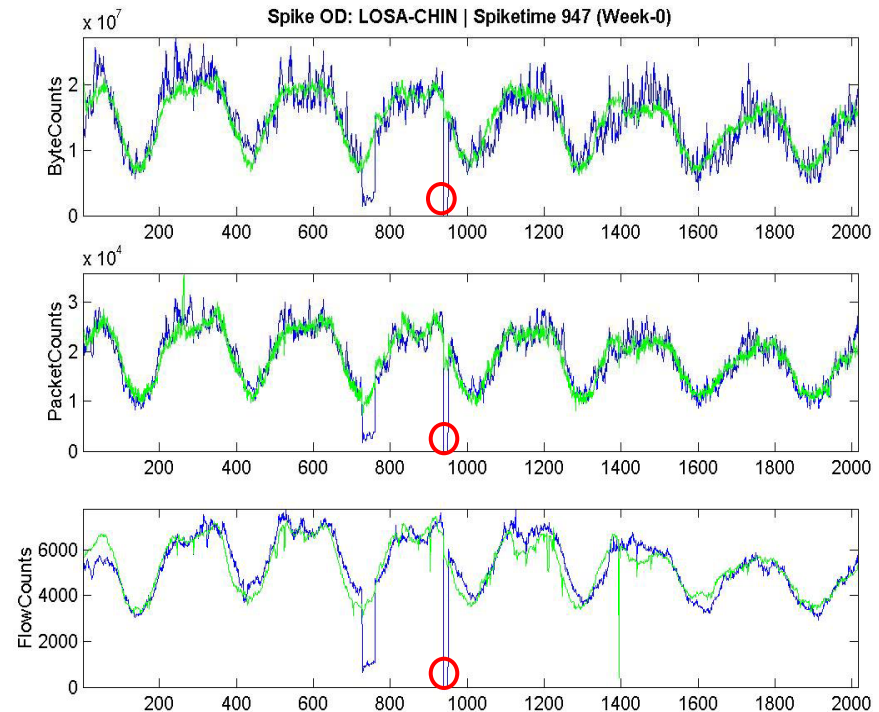
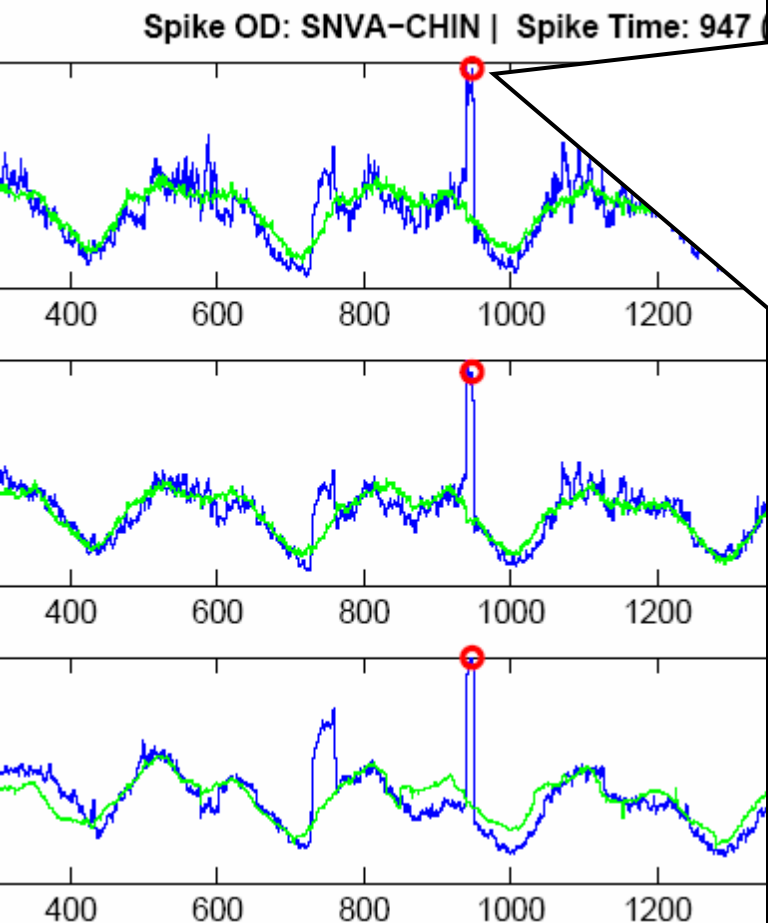
# An example BP anomaly (heavy flow)



# An example PF anomaly (DOS attack)



# An example BPF Anomaly (ingress-shift)

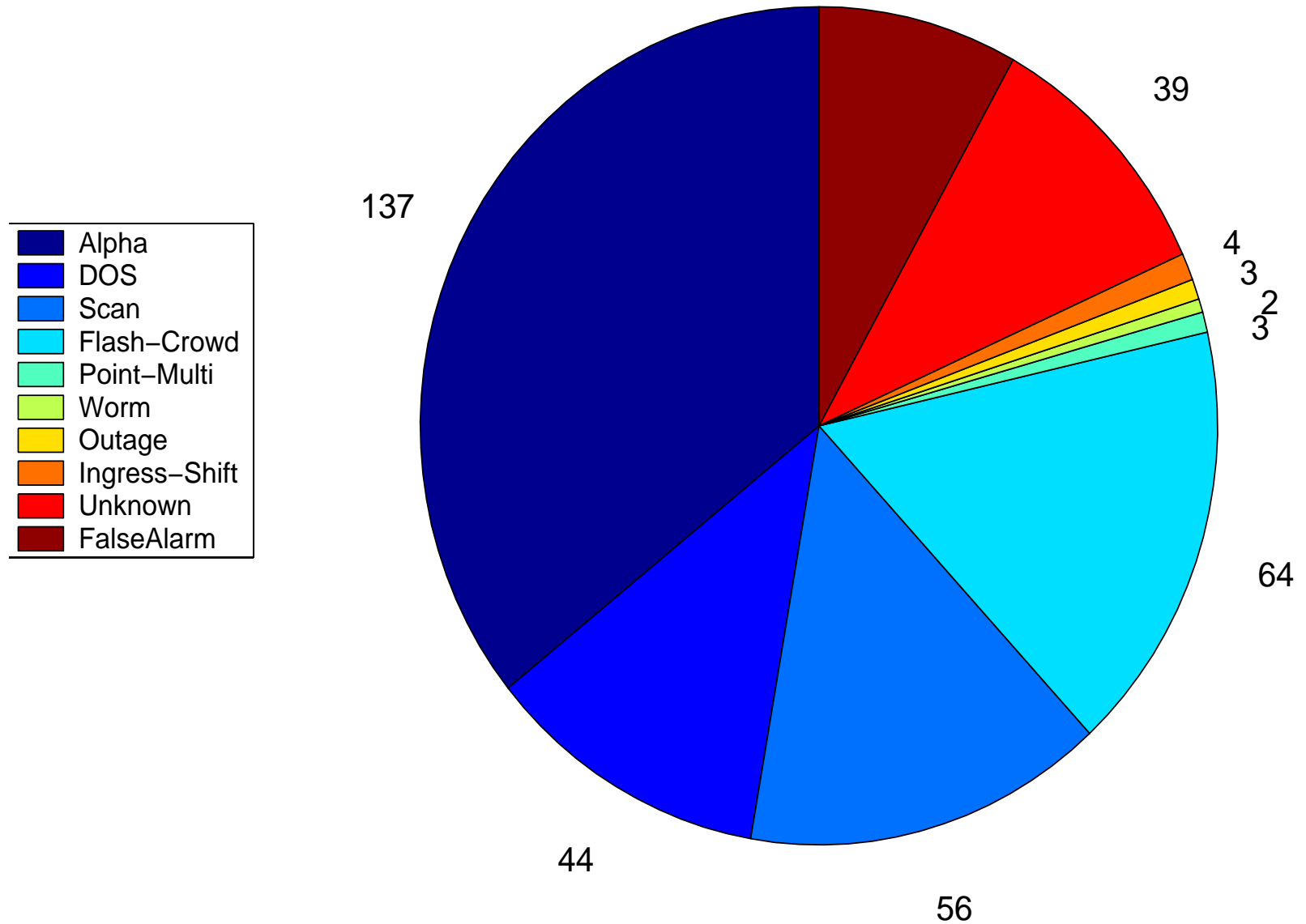


Multihomed customer CALREN reroutes around the LOSA-CHIN (scheduled) outage

# Species of anomalies found

Anomaly	Definition
ALPHA	Unusually high rate point to point byte transfer
DOS, DDOS	(Distributed) Denial of service attack against a single victim
FLASH CROWD	Unusually large demand for a resource/service emerging from common set of sources
SCAN	Scanning a host for a vulnerable port (port scan) or scanning the network for a target port (network scan)
WORM	Self-propagating code that spreads across a network by exploiting security flaws
POINT to MULTIPOINT	Distribution of content from one server to many servers
OUTAGE	Equipment related events that decrease traffic exchanged by an OD pair
INGRESS-SHIFT	Customer shifts traffic from one ingress point to another

# Summary of Anomalies Found 31





# Conclusions

- Subspace method for anomaly diagnosis allows whole-network approach
  - Significant benefit accrues from whole-network analysis
- Diagnosing Volume Anomalies from Link Traffic:
  - High detection rate, low false alarm rate
  - Hypothesis-based identification is easily formalized and extended
- Detecting General Anomalies from Flow Traffic:
  - Anomalies detected span remarkable breadth
  - Almost all of the anomalies found are operationally relevant
- Whole-Network Anomaly Diagnosis with the Subspace Method is promising
  - ... more to come!

# Thanks!



## Help with Abilene Data

- Rick Summerhill, Mark Fullmer (Internet2)
- Matthew Davy (Indiana University)

## Help with Sprint-Europe Data



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